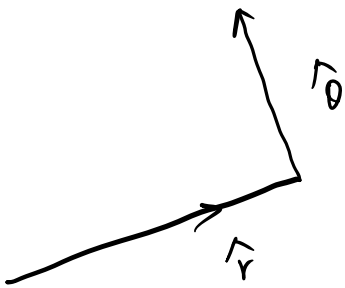


I. Centripetal force \rightarrow Gravity

向心力

A Centripetal force is that by which bodies are drawn or impelled, or any way tend, towards a point as to centre. « mathematical principles of natural philosophy »



如何确定矢量的方向？

$$\vec{r} = x \hat{i} + y \hat{j} \quad (\text{位置矢量描述})$$

projection: $\vec{r} \cdot \hat{i} = x$

$$\vec{r} \cdot \hat{j} = y$$

$\vec{r}(x, y)$ 也可以写为 $\vec{r}(r, \theta)$

$$\hat{i} = \lim_{\Delta x \rightarrow 0} \frac{\vec{r}(x+\Delta x, y) - \vec{r}(x, y)}{|\vec{r}(x+\Delta x, y) - \vec{r}(x, y)|}$$

x 方向变化量为 Δx

同理定义 \hat{j}

(可以考虑提及 partial)

以类似的方式看待

$$\hat{r} = \lim_{\Delta r \rightarrow 0} \frac{\vec{r}(r+\Delta r, \theta) - \vec{r}(r, \theta)}{|\vec{r}(r+\Delta r, \theta) - \vec{r}(r, \theta)|}$$

$$\hat{\theta} = \lim_{\Delta \theta \rightarrow 0} \frac{\vec{r}(r, \theta+\Delta \theta) - \vec{r}(r, \theta)}{|\vec{r}(r, \theta+\Delta \theta) - \vec{r}(r, \theta)|}$$

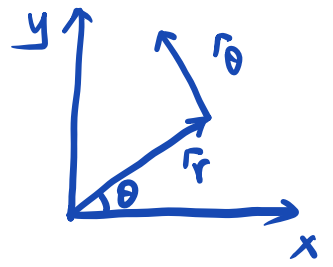
由此可见 $\hat{\theta}$ 的方向。

讨论随时间的变化率。

1° 几何作图法

2° 三角函数微分法

$$\begin{aligned}\vec{r} &= x\hat{x} + y\hat{y} = r\hat{r} \\ &= r\cos\theta\hat{x} + r\sin\theta\hat{y}\end{aligned}$$



以 \hat{x} , \hat{y} 为
基, 它们
随时间变化

$$\hat{x} = \cos\theta \hat{x} + \sin\theta \hat{y}$$

$$\hat{y} = -\sin\theta \hat{x} + \cos\theta \hat{y}$$

$$\begin{aligned} \frac{d\hat{x}}{dt} &= -\sin\theta \frac{d\theta}{dt} \hat{x} + \cos\theta \frac{d\theta}{dt} \hat{y} \\ &= \frac{d\theta}{dt} \hat{y} \end{aligned}$$

$$\begin{aligned} \frac{d\hat{y}}{dt} &= -\cos\theta \frac{d\theta}{dt} \hat{x} - \sin\theta \frac{d\theta}{dt} \hat{y} \\ &= -\frac{d\theta}{dt} \hat{x} \end{aligned}$$

推广至一般情形

$$\vec{r}(r, \theta)$$

$$(\hat{x} \cdot \hat{y} = 0)$$

$$\vec{r} = r \hat{x}$$

$$\frac{d\vec{r}}{dt} = \frac{dr}{dt} \hat{x} + r \frac{d\theta}{dt} \hat{y}$$

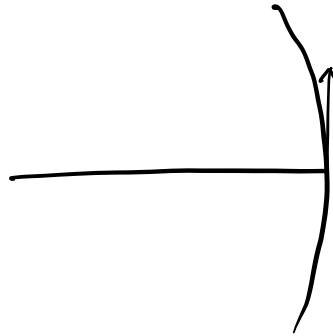
匀速圆周运动 \downarrow

$$= 0 + \omega r \hat{y}$$

$$= v \hat{y} \quad (\text{切向})$$

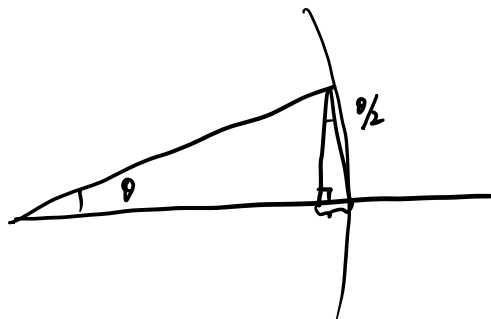
则求 $\vec{a} = \frac{d^2\vec{r}}{dt^2}$

Q: A car why doesn't fall down?



Circular motion with a certain speed v falls away from a straight line path by a distance equal to $\frac{1}{2}(v^2/R)t^2$ if t is very small.

If I move on in this way,



$$\text{Chord} : R \theta$$

$$R \theta \sin \frac{\theta}{2}$$

$$R \omega t \sin \frac{\omega t}{2}$$

$$\approx \frac{1}{2} R \omega^2 t^2 = \frac{1}{2} a t^2$$

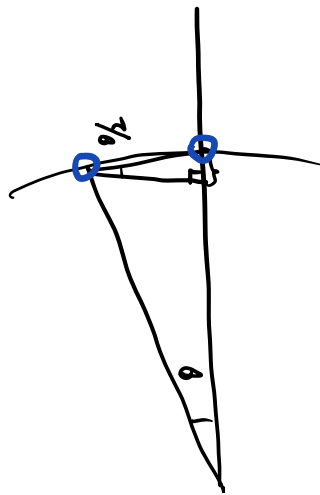
\vec{a} is changing

check differential / integral

$$\begin{aligned} & \int_0^t R d\theta \sin\theta \\ &= R (1 - \cos\omega t) \\ &= 2R \sin^2 \frac{\omega t}{2} \\ &= \frac{1}{2} \omega^2 R t^2 \end{aligned}$$

The same reason applies to the moon

It is also the greatness of Newton



換想一下，月亮就是
在往下掉的

(是不是很像平拋運動)

2° 弹性力 (elastic force)

$$F = -kx \quad \begin{array}{l} \nearrow \text{displacement} \\ \text{Hooke's law} \end{array}$$

(restore force)

讨论简谐运动的基础

3° 表面张力

属于基本相互作用力中的：电磁相互作用

(相互靠近的原子或分子之间作用力的宏观表现)

IV: Nuclear force

$\sim 10^{-15} \text{ m}$, very small

comp: $\text{\AA} = 10^{-10} \text{ m}$ (quantum mechanics)

Strong / weak (even shorter force range)
smaller force
↓
keep the objects stable (束缚) ↓ occur in some reactions
e.g. β -decay

in the sense of high energy (250 GeV)

Weinberg / Salam / Glashow (late 1960s) unification of electromagnetic and weak force

↓ when the energy is decreased
the spontaneous symmetry breaking
电 / 弱

弱或电两种性质极不相同的相互作用

note: In nuclear analysis, we no longer think in terms of forces, and in fact we can replace the force concept with a concept of the energy

of interaction of two particles.

(平方反比力, Newton不是第一个发现
但第一个证明)

拓展: Fields

$$G \frac{m_1 m_2}{r^2}$$

vs

$$\frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2}$$

Rules of reasoning in philosophy

哲学中的推理法则

Rule 1 We are to admit no more causes
of natural things than such as are both
true and sufficient to explain their
appearances.

除那些真实而已足够说明其现象者外,
不必去寻求自然界事物的其他原因

“自然界不做无用之事”

To this purpose the philosophers say that
Nature does nothing in vain, and more

is in vain when less will serve; for

Nature is pleased with simplicity, and

affects not the pomp of superfluous

causes.

↓
夸耀

/su: 'pɔ: flʌs/
多余的, 不必要的

pompous 浮夸的

少够用多即是无用；自然界喜欢

简单化，而不爱用什么多余的原因

以夸耀自己。

Rule II Therefore to the same natural effects we must, as far as possible, assign the same causes.

所以对于自然界中同一类结果，必须尽可能归之于同一种原因。

例如人和牲畜的呼吸；
陨石在欧洲和美洲的下落；
炉火和太阳的光；
光线在地球和行星上的反射。

Rule II

The qualities of bodies, which admit neither intensification nor remission of degrees, and which are found to (分开为 found to 吗?)

belong to all bodies within the reach of our experiments, are to be esteemed the universal qualities of all bodies whatsoever.

物体的属性，凡既不能增强也不能减弱者，又为我的实验所能及的范围内的一切物体所具有者，就应视为所有物体的普遍属性。

Rule IV

in experimental philosophy we are to
look upon ^{命题} propositions inferred by general
induction from phenomena as accurately
or very nearly true, notwithstanding ^{尽管}
any contrary hypotheses that may be
imagined, till such time as other
phenomena occur, by which they
may either be made more accurate,
or liable ^{有责任的} to exceptions.

在实验哲学中，我们必须把那些从各种现象中运用
一般归纳而导出的命题看作是完全正确的，或者是非常
接近正确的；虽然可以想象出与之相反的假说，但是没有
出现其他现象使之变更准确或面临意外前，视归纳命题正确。